

# **Log(v) 3LPF: A linearized solution to train reinforcement learning algorithms for distribution systems**

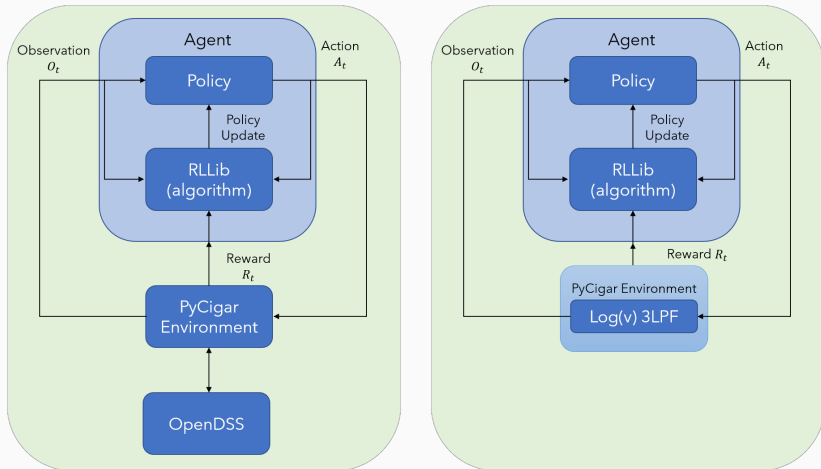
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Arizona State University

# Reinforcement learning on distribution systems, PPO-Clip



**Figure 1:** Current PyCigar modeling diagram (left) vs proposed architecture (right)

# Reinforcement learning on distribution systems, PPO-Clip

- Two neural networks. Weights obtained via SGD
  - Policy function:  $\theta_{k+1} = \arg \min_{\theta} g(\hat{R}_t, s_{rl}, a_{rl}, \theta)$
  - Value function:  $\phi_{k+1} = \arg \min_{\phi} h(\hat{R}_t, s_{rl}, a_{rl}, \phi)$
- Power Flow (PF) equations are used to compute the rewards
- Rewards are computed for every training iteration, every time step and every action sampled by the algorithm
- **Efficient** and **accurate** PF solvers are necessary

**Our target:**  $\rightarrow \boxed{\hat{R}_t = f(s_p^1, s_{rl}^2, a_{rl}^3)}$

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<sup>1</sup> $s_p$ : Power system state

<sup>2</sup> $s_{rl}$ : Reinforcement learning state

<sup>3</sup> $a_{rl}$ : Reinforcement learning action

# Distribution systems are unbalanced

- Unbalanced system  $\rightarrow$  3-phase solvers
- Need for AC modeling vs DC
  - AC PF equations are **non-linear**
  - Non-linearity is caused by ZIP load models (details later)
- Modeling of line losses through shunt elements (not negligible) needed

PF formulations:

$$\text{Current: } \mathbf{i} = \mathbf{Y}_{\text{bus}} \mathbf{v}$$

$$\text{Power: } \mathbf{s} = D(\mathbf{v} \mathbf{v}^H \mathbf{Y}_{\text{bus}}^H)$$

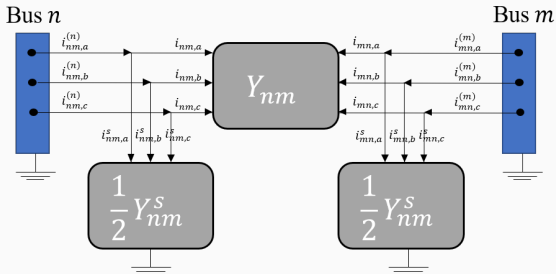


Figure 2: Pi-Model representation

# Survey of ACPF solvers

- Commercial software PF solvers are **iterative**
  - Newton-Raphson (GridLab-D, PSLF)
  - Gauss-Seidel (OpenDSS, GridLab-D)
  - Forward-Backward Sweep (GridLab-D)
- Previous work, linear approximations
  - Lin3DistFlow [[Sankur et al., 2016](#)]. Nominal voltages and no losses. No ZIP models
  - NFA [[Fobes et al., 2020](#)]. Real-power only, no ZIP models
  - DCP [[Fobes et al., 2020](#)]. DC assumption, ignores reactive power, no ZIP models
  - Lossy Distflow [[Schweitzer et al., 2019](#)]. Not valid for complete ZIP models, cannot accommodate modeling of transformers, regulators, losses are parametrized.
  - **LPF** [[Li et al., 2017](#)]. Positive-sequence only, lossless, no ZIP models, doesn't exploit tree structure (use case is transmission systems).

# Our contribution

- **Modeling capabilities**

- Embedded linear power flow solver
- ZIP load models, shunt capacitors, regulators, transformers, smart inverters, batteries, and corresponding controls (as of today).
- Ability to fully control and understand unbalanced 3-phase distribution systems. Implementation of new attack vectors
- Linear PF and OPF. Applicable to transmission systems.

- **Modeling accuracy**

- PF solution validated against OpenDSS
- Modeling of devices matches that of OpenDSS

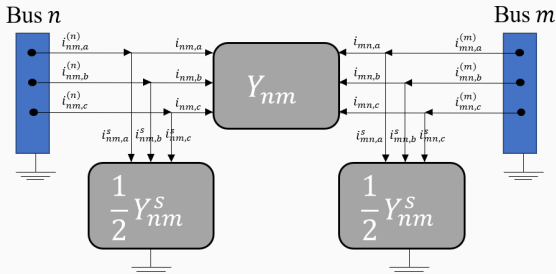
- **Computational complexity**

- Linear equations allow to solve the system in a single snapshot. In OpenDSS, IEEE-13 11 iterations, IEEE-8500 62 iterations reducing RL training times
- Ability to exploit graph tree structure
- Ability to efficiently compute inverse after perturbation
- Reduced overhead due to api calling external models

**Log(v) 3LPF**

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# Log(v) 3LPF



**Kirchoff:**  $\mathbf{i}_{nm}^{(n)} = \mathbf{i}_{nm} + \mathbf{i}_{nm}^s$

**Ohm:**  $\mathbf{i}_{nm} = \mathbf{Y}_{nm}^{(n)} \mathbf{v}_n - \mathbf{Y}_{nm}^{(m)} \mathbf{v}_m$

**Losses:**  $\mathbf{i}_{nm}^s = \frac{1}{2} \mathbf{Y}_{nm}^s \mathbf{v}_n$

$$\mathbf{i}_{nm}^{(n)} = \left( \mathbf{Y}_{nm}^{(n)} + \frac{1}{2} \mathbf{Y}_{nm}^s \right) \mathbf{v}_n - \mathbf{Y}_{nm}^{(m)} \mathbf{v}_m$$

$$\mathbf{S}_{nm}^{(n)} = \mathbf{v}_n \left( \mathbf{i}_{nm}^{(n)} \right)^H$$

$$\mathbf{S}_{nm}^{(n)} = \mathbf{v}_n \mathbf{v}_n^H \left( \mathbf{Y}_{nm}^{(n)} + \frac{1}{2} \mathbf{Y}_{nm}^s \right)^H - \mathbf{v}_n \mathbf{v}_m^H \left( \mathbf{Y}_{nm}^{(m)} \right)^H$$



$$\mathbf{S}_{nm}^{(n)} = \mathbf{v}_n \mathbf{v}_n^H \left( \mathbf{Y}_{nm}^{(n)} + \frac{1}{2} \mathbf{Y}_{nm}^s \right)^H - \mathbf{v}_n \mathbf{v}_m^H \left( \mathbf{Y}_{nm}^{(m)} \right)^H$$

We want to remove the non-linearity  $\mathbf{v}_n \mathbf{v}_n^H$  from the equation that relates power flows to voltage

$$\mathbf{v}_n := [v_n^a, v_n^b, v_n^c]^T, \quad v_n^p = |v_n^p| e^{j\theta_p} \quad (1)$$

$$|v_n^p| = e^{\log|v_n^p|}, \quad u_n^p := \log|v_n^p| \quad (2)$$

$$v_n^p = e^{u_n^p} e^{j\theta_p} \quad (3)$$

$$\mathbf{S}_{nm}^{(n)} = \mathbf{v}_n \mathbf{v}_n^H \left( \mathbf{Y}_{nm}^{(n)} + \frac{1}{2} \mathbf{Y}_{nm}^s \right)^H - \mathbf{v}_n \mathbf{v}_m^H \left( \mathbf{Y}_{nm}^{(m)} \right)^H$$

We know voltages are around 1 p.u., thus  $\log(1) = 0$ , and we approximate the voltage magnitude in  $v_n^p = e^{u_n^p} e^{j\theta_p}$  using first-order Taylor expansion.

$$\mathbf{v}_n := \begin{pmatrix} e^{u_n^a} e^{j\theta_n^a} \\ e^{u_n^b} e^{j\theta_n^b + \frac{2\pi}{3} - \frac{2\pi}{3}} \\ e^{u_n^c} e^{j\theta_n^c - \frac{2\pi}{3} + \frac{2\pi}{3}} \end{pmatrix} = \Delta_3 \text{diag} \begin{pmatrix} e^{u_n^a} \\ e^{u_n^b} \\ e^{u_n^c} \end{pmatrix} \begin{pmatrix} e^{j\tilde{\theta}_n^a} \\ e^{j\tilde{\theta}_n^b} \\ e^{j\tilde{\theta}_n^c} \end{pmatrix} \quad (4)$$

$$\mathbf{v}_n \approx \Delta_3 (\mathbf{I} + \text{diag}(\mathbf{u}_n)) e^{j\tilde{\theta}_n} \quad (5)$$

$$\begin{aligned} \mathbf{v}_n \mathbf{v}_n^H &\approx \Delta_3 \left( \mathbf{1}\mathbf{1}^T + \mathbf{u}_n \mathbf{1}^T + \mathbf{1}^T \mathbf{u}_n^T + j\tilde{\theta}_n \mathbf{1}^T - j\mathbf{1} \tilde{\theta}_n^T \right) \Delta_3^H \\ \mathbf{v}_n \mathbf{v}_m^H &\approx \Delta_3 \left( \mathbf{1}\mathbf{1}^T + \mathbf{u}_n \mathbf{1}^T + \mathbf{1}^T \mathbf{u}_m^T + j\tilde{\theta}_n \mathbf{1}^T - j\mathbf{1} \tilde{\theta}_m^T \right) \Delta_3^H \end{aligned} \quad (6)$$

$$\text{Non-linear ACPF: } \mathbf{S}_{nm}^{(n)} = \mathbf{v}_n \mathbf{v}_n^H \left( Y_{nm}^{(n)} + \frac{1}{2} Y_{nm}^s \right)^H - \mathbf{v}_n \mathbf{v}_m^H \left( Y_{nm}^{(m)} \right)^H$$

Reordering and defining the corresponding matrices and vectors

**Log(v) 3LPF (Linear):**

$$\tilde{\mathbf{s}}_{nm} \approx \tilde{\mathbf{Y}}_{\text{bus}} \mathbf{x} \quad \text{where} \quad \mathbf{x} \triangleq \begin{bmatrix} \mathbf{u} \\ \tilde{\boldsymbol{\theta}} \end{bmatrix} \quad (7)$$

$$\mathbf{x} \approx \tilde{\mathbf{Y}}_{\text{bus}}^{-1} \tilde{\mathbf{s}}_{nm}$$

and we may recover the voltage phasors as follows

$$\mathbf{v} \approx \Delta_3 \text{diag}(e^{\mathbf{u}}) e^{j\tilde{\boldsymbol{\theta}}_n}$$

## ZIP models

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# ZIP models. Wye-connected loads

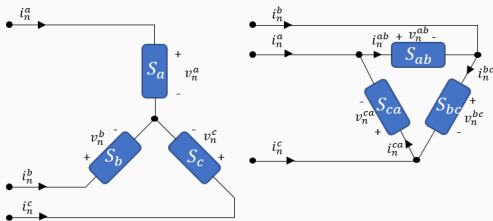


Figure 3: Wye (left) and delta-connected (right) load

Wye-connected loads:  $S_n^Y = S_n^{Z,Y} + S_n^{I,Y} + S_n^{P,Y}$

$$\mathbf{Z}: S_n^{Z,Y} = (y_n^Y)^* + 2\text{diag}(y_n^Y)^* \mathbf{u}_n$$

$$\mathbf{I}: S_n^{I,Y} \approx \Delta_3 (i_n^Y)^* + \Delta_3 \text{diag} (i_n^Y)^* \mathbf{u}_n + j\Delta_3 \text{diag} (i_n^Y)^* \tilde{\theta}_n$$

$$\mathbf{P}: S_n^{P,Y} = s_\ell^Y$$

# ZIP models. Delta-connected loads

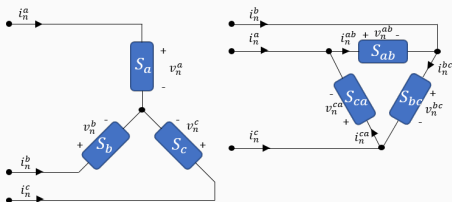


Figure 4: Wye (left) and delta-connected (right) load

Delta-connected loads:  $S_n^\Delta = S_n^{Z,\Delta} + S_n^{I,\Delta} + S_n^{P,\Delta}$

$$\mathbf{Z}: S_n^{Z,\Delta} \approx \left( \text{diag} \left( \Delta_3 \left( \tilde{Y}_n^\Delta \right)^T \mathbf{1} \right) + \Delta_3 \left( \tilde{Y}_n^\Delta \right)^T \right) \mathbf{u}_n \\ + \left( \text{diag} \left( \Delta_3 \left( \tilde{Y}_n^\Delta \right)^T \mathbf{1} \right) - \Delta_3 \left( \tilde{Y}_n^\Delta \right)^T \right) \tilde{\boldsymbol{\theta}}_n$$

$$\mathbf{I}: S_n^{I,\Delta} \approx \Delta_3 \Lambda \left( \mathbf{i}_n^Y \right)^* + \Delta_3 \text{diag} \left( \Lambda \mathbf{i}_n^Y \right)^* \mathbf{u}_n + j \Delta_3 \text{diag} \left( \Lambda \mathbf{i}_n^Y \right)^* \tilde{\boldsymbol{\theta}}_n$$

$$\mathbf{P}: S_n^{P,\Delta} \approx \Lambda s_\ell^\Delta$$

# Modeling and control of power delivery elements

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# Transformers and voltage regulators

Modeled through the **admittance matrix**

$$S_{nm}^{(n)} = \mathbf{v}_n \mathbf{v}_n^H \left( \mathbf{Y}_{nm}^{(n)} + \frac{1}{2} \mathbf{Y}_{nm}^s \right)^H - \mathbf{v}_n \mathbf{v}_m^H \left( \mathbf{Y}_{nm}^{(m)} \right)^H$$

**Transformers:**

$$\mathbf{Y}_{\text{prim}} = \mathbf{A} \mathbf{N} \mathbf{B} \left( \mathbf{Z}_{nm}^t \right)^{-1} \mathbf{B}^T \mathbf{N}^T \mathbf{A}^T$$

$$\mathbf{Y}_{\text{prim}} = \begin{pmatrix} \mathbf{Y}_{nm}^{(n)} & \mathbf{Y}_{nm}^{(m)} \\ \mathbf{Y}_{mn}^{(n)} & \mathbf{Y}_{mn}^{(m)} \end{pmatrix}$$

**Voltage regulators:**

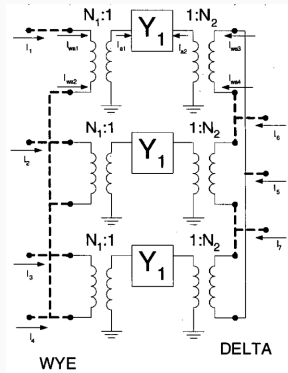
$$\mathbf{Y}_{\text{prim}} = \mathbf{\Gamma} \mathbf{A} \mathbf{N} \mathbf{B} \left( \mathbf{Z}_{nm}^t \right)^{-1} \mathbf{B}^T \mathbf{N}^T \mathbf{A}^T \mathbf{\Gamma}^T$$

where  $\mathbf{\Gamma} = \text{diag}(\gamma)$  and  $\gamma_i = 1 \pm 0.00625 \tau_i$

$$\tau_i = f(v_{\text{reg}}, v_b, v_n)$$

**Attack vectors**

$v_{\text{reg}}$  setpoint,  $v_b$  bandwidth,  $v_n$  measurement



**Figure 5:** WyeG-Delta Transformer



# Shunt capacitors and cap controls

Modeled as a wye or delta-connected **constant impedance load**

$$\boxed{S_n^{Z,Y} = D \left( \mathbf{v}_n \mathbf{v}_n^H \mathbf{\Pi} \left( \mathbf{Y}_n^Y \right)^H \mathbf{\Pi}^T \right)} \quad \text{or} \quad \boxed{S_n^{Z,\Delta} = D \left( \mathbf{v}_n \mathbf{v}_n^H \mathbf{\Pi} \left( \mathbf{Y}_n^\Delta \right)^H \mathbf{\Pi}^T \right)}$$

**Capacitor banks:**

$$\mathbf{Y}_n^Y = \text{diag} \left( \mathbf{y}_n^Y \right), \quad \mathbf{Y}_n^\Delta = \text{diag} \left( \mathbf{y}_n^\Delta \right),$$
$$\mathbf{y}_n^Y = [y_{n,a}^Y, y_{n,b}^Y, y_{n,c}^Y]^T, \quad \mathbf{y}_n^\Delta = [y_{n,a}^\Delta, y_{n,b}^\Delta, y_{n,c}^\Delta]^T$$

**Cap controls:**

$$\mathbf{y}_n^Y = \sum_{i=1}^{n_c^s} \eta_{c,i} \mathbf{y}_{c,i}^Y, \quad \mathbf{y}_n^\Delta = \sum_{i=1}^{n_c^s} \eta_{c,i} \mathbf{y}_{c,i}^\Delta$$

$$\text{where } n_c^s \rightarrow \text{N steps, } \eta_{c,i} \in \{0, 1\} \quad \eta_{c,i} = f(\vartheta^4, \boxed{\bar{\vartheta}, \underline{\vartheta}^5})$$

<sup>4</sup>Control input (current, voltage, kvar, PF, time)

<sup>5</sup>Attack vector. Upper and lower limits (operation is outside limits)

Modeled as a wye-connected **constant power load**

$$S_n^{P,Y}(t) = s_\ell^Y(t)$$

**Solar resources and batteries:**

$$S_n^{P,Y}(t) = s_\ell^Y(t) \quad \text{and} \quad S_n^{P,Y}(t) = f(\eta_{c,t}, \eta_{d,t}, s_{oc}(t-1))^6$$

**Smart Inverters:**

$$S_n^{P,Y}(t) = f(s_\ell^Y(t-1), v_{n,t}^7)^8$$

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<sup>6</sup>State of charge

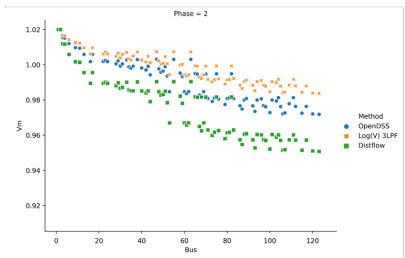
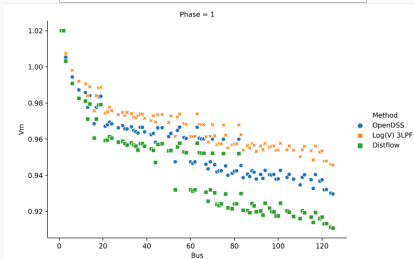
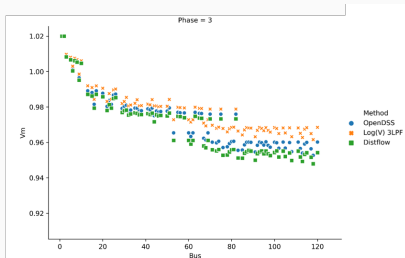
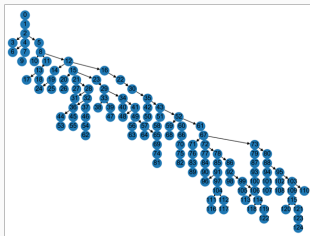
<sup>7</sup>Voltage measurement

<sup>8</sup>Attack vector. Changes in drop curve settings

## Preliminary results

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# IEEE-123 test case



# OpenDSS vs Log(V) 3LPF

RMSE (IEEE-123)	Distflow	Log(V) 3LPF
Phase 1	0.014	0.012
Phase 2	0.016	0.08
Phase 3	0.006	0.04

Case	Devices	Buses	Nodes	Losses (%)
IEEE-123	238	132	278	2.63
IEEE-8500	7282	4876	8531	10.58
European LV	965	907	2721	0.2703

Case	Iterations	OpenDSS (s)	Log(V) 3LPF (s)
IEEE-123	3	0.011	0.001
IEEE-8500	62	0.244	n/a
European LV	3	0.087	n/a

- Exploring techniques to solve the linear system of equations. E.g.
  - Forward-backward sweep
  - Truncated SVD
  - Parallel computation on leaf nodes
- Re-centering around 1 to obtain better approximation
- Sherman-Morrison for matrix inversion after perturbation
- Solving large cases directly from .dss files

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**Powermodelsdistribution. jl: An open-source framework for exploring distribution power flow formulations.**

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Li, Z., Yu, J., and Wu, Q. (2017).

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Schweitzer, E., Saha, S., Scaglione, A., Johnson, N. G., and Arnold, D. (2019).

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